A hinged-pad test structure for sliding friction measurement in micromachining

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ABSTRACT

We describe the design, modeling, fabrication and initial testing of a new test structure for friction measurement in MEMS. The device consists of a cantilevered forked beam and a friction pad attached via a hinge. Compared to previous test structures, the proposed structure can measure friction over much larger pressure ranges, yet occupies ten to one hundred times less area. The placement of the hinge is crucial to obtaining a well-known and constant pressure distribution in the device. Static deflections on the device were measured and modeled numerically. Preliminary results indicate that friction pad slip is sensitive to friction pad normal force.

Keywords: sliding friction, test structure design, interferometric measurement, numerical simulation

1. INTRODUCTION

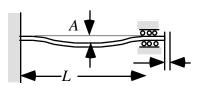
In Microelectromechanical Systems (MEMS), surface forces can play a relatively large role compared to gravity and inertia, which are the dominating forces at the macroscale. Because surface forces are not well characterized and often difficult to reproduce in MEMS structures, most commercial applications avoid contact between structural members. Examples include accelerometers and gyroscopes [1-3]. An important commercial device in which *adhesive contact* between moving structures and the substrate is allowed is the Digital Mirror Device [4]. For this product, adhesion (e.g., stiction) and adhesion hysteresis (changes in adhesion over time or due to environment) are important factors in determining device reliability. While great reliability improvement has necessarily been achieved through testing of full scale devices [5], these surface properties can also be studied through the use of test structures [6-8]. From such studies, we hope to understand and control surface forces in micromachine structures, which may permit us to take advantage of surface characteristics in micromachine design.

If sliding contact between structural members is allowed, a large new class of devices can be brought to product realization in MEMS. Examples include gears for mirror rotation [9], pop-up mirrors and linear racks [10], and shuffle motors [11]. However, relatively little is understood regarding the friction laws of such devices in contact, such as how friction may scale with apparent pressure or sliding velocity. These parameters can vary by orders of magnitude: 0.1 to 100 MPa in apparent pressure and 0.1 to 1000 µm/sec in velocity, depending on the application. In larger scale devices, friction can depend strongly on these factors [12]. Information on friction of horizontal surfaces in MEMS has been obtained using reciprocating comb drive structures [13-14]. According to these data, the coefficient of friction (cof) ranges from about 2-5 for oxide coated polycrystalline silicon (polysilicon) devices to 0.1 for polysilicon devices coated with hydrophobic films. Applied pressures were in the tens of kilopascals. Because the force generated by comb drives is on the order of micronewtons, only a small normal pressure range can be studied for a given test structure. Further, the comb drive consumes a large area to obtain the friction data. In this paper, we consider cantilever beams as potential friction devices. Forces generated can vary from the micronewton to the millinewton level. Hence, a much larger pressure range can potentially be explored at the expense of slip range. Also, with their small footprint, such devices have the potential to serve as parametric test structures. That is, they can provide valuable information without occupying significant real estate on chips, acting as in-situ diagnostic process monitors.

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[†] We distinguish between apparent and true pressure. Apparent pressure is that which can be calculated from contact mechanics assuming smooth surfaces. Actual pressure is that which occurs locally when surface roughness is taken into account. In MEMS, surface texturing of 2-10 nm rms depending on processing of the structural material, give rises to local pressures at asperity tips 10 to 100 times greater than apparent pressure.

2. CONCEPTUAL EVOLUTION OF THE TEST STRUCTURE



For an inextensible beam, out-of-plane force applied to a cantilever beam induces slip , according to the relationship

$$=c\frac{A^2}{L}. (1)$$

deflection of amplitude A.

Fig. 1 Slip induced by out-of-plane Here, A is the amplitude of the deflection, L is the length of the beam, and the constant c 2 to first order. The slip is small for such a design; we shall see that it is on the order of 15 nm. An

average contact radius between asperities of 10 nm has been calculated for the rms roughness typical of our polysilicon [15]. Therefore, while the slip is small, it should be sufficient to disengage contacting asperities, and engage asperities at new contacts. Hence, it seems reasonable to expect that a properly designed cantilever structure can incur losses typical of frictional processes in micromachines.

Our goal is to design a friction device which meets the criteria of having independent pressure and velocity control. Although the slip for a cantilever beam is small, the force generated can be very large. Therefore, it should be possible to apply a large range of pressures if the device is properly designed. Velocity can be controlled through the frequency of the applied force to the driver beam.

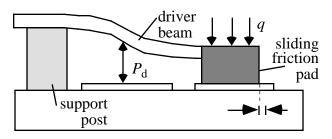


Fig. 2a First concept for friction test structure. This structure fails because the slider block cannot be uniformly maintained in contact with the substrate as driver force P_d cycles.

Our first attempt at building a test structure is conceptually represented in Fig. 2a. The driver beam is initially flat and suspended above the substrate, being cantilevered from the support post at the left end. The friction pad is brought into contact by the distributed load q. Oscillating force P_d will cause the slider to move back and forth, with contact area controlled by the design length of the friction pad. Both q and P_d are generated by electrostatic forces.

Because of the restoring force of the cantilever, the force q applied to the slider pad cannot immediately cause uniform contact. Beam theory was utilized to understand the deflections in the slider pad area as a

function of P_d. For this test structure design, we found that the slider pad could not be maintained in contact along its length as P_d varied, even for large values of q. At P_d =0, this was physically traced to the connection between the end of the cantilever and the friction pad. To keep the pad in contact along its entire length, the slope must be 0 at this connection. Enforcement of this condition requires that a moment exist at the connection. However, as the pad becomes flat with increasing q, the moment vanishes. For example, when applying 40V to generate a q of 7,000 N/m^2 , the length along the friction pad which is not touching is approximately 30 microns for $P_d = 0$. As P_d increases, the pad eventually does come perfectly into contact. But for subsequent increase of P_d , the friction pad

hinge pivot $P_{\rm d}$ 3.9 µm $6 \mu m$

Fig. 2b Improved friction test structure. By connecting to the friction pad via a hinge, a virtually uniform pressure is achieved for relatively small values of q.

rocks about its left bottom corner, leaving only a point contact.

We improved the design as seen in Fig. 2b. Relative to Fig. 2a, the structure differs only in its connection between the sliding friction pad and the driver beam, in that now the connection is made by a hinge. The hinge placement allows the contact area of the pad to be virtually independent of P_d . This is for two reasons: First, at P_d =0, the force applied by q on both sides of the hinge allows the slope at the connection point to approach 0 at relatively low values of q. Second, as P_d increases for a given value of q, rocking is resisted

because the hinge placement allows the friction pad to extend to the left of the connection between the driver beam and the pad.

The layout and design of the structure is shown in Fig. 3. Fig. 3a is a top view, where it is seen that the hinge is formed by forking the driver beam around the friction pad. In the present work, the length of the driver beam L_d is 500 μ m, the length of the friction pad L_p is 200-600 μ m, and the length of the hinge L_h is 10 μ m. This hinge length is sufficient to be "stiff", that is, it twists only a small amount due to its high polar moment of inertia.

 L_h can be shortened to 2 μ m such that the hinge becomes flexible. This further reduces the change in contact area vs. P_d . However, according to our calculations, axial compliance of a flexible hinge can be a nm or more for large cof. Because the slip $\,$ is only about 15 nm, this can reduce the actual slip of the friction pad. The width of the driver beam W_d is 50 μ m to maximize the axial force developed by the driver beam. The width of the hinge W_h is 5 μ m to minimize its torsional and lateral compliance.

Fig. 3b shows a cross-sectional schematic view after poly 3 etch of the friction pad area through section AA' of Fig. 3a. Four levels of polysilicon (poly), designated as P0, P1, P2, and P3 are used to form this part of the structure. Sacrificial oxide layers are designated as SO1, SO2 and SO3. Voltage applied across the poly 1 pad to the electrostatic wings in poly 3 provides normal distributed force q to bring the friction pad into contact with poly 0 at a few volts. Once this occurs, the friction pad acts as a stop, and subsequent voltage applied to poly 1 supplies controllable normal pressure. In this structure, poly 1 is not a necessity; poly 0 could be used instead. However, because of the inverse square relationship of electrostatic force with gap distance, the use of poly 1 allows much higher normal forces to be applied at a given voltage. By taking advantage

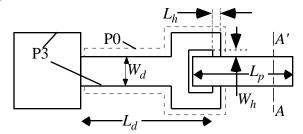


Fig. 3a Top view of the hinged friction pad P3 - poly 3, P0 - poly 0.

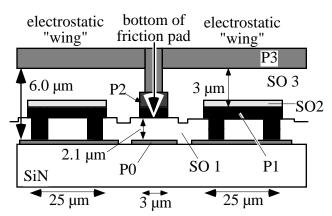


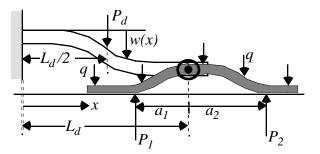
Fig. 3b Cross-section through AA' of Fig. 3a. P - poly, SO - sacrifical oxide.

of conformality in polysilicon deposition, fabrication of the friction pad with a $6 \mu m$ thick beam is possible. This creates a highly uniform pressure across the width of the sliding friction pad because its flexure is extremely small when loaded by the electrostatic wings.

3. ANALYTICAL MODELING

To derive quantitative trends regarding controllability of the contact area, distributed loading q was assumed in the friction pad region, and point loading P_d was applied to the driver pad, as shown in Fig. 4a. The point loading allows simple analytical modeling to be utilized, and deformation trends can be predicted. In the actual experimental situation of Fig. 3a, distributed electric field loading is applied across the driver beam – this will be numerically modeled in the testing section below.

Initially the friction pad is suspended above the surface. As q is increased, it comes into contact with the substrate. Referring to Fig. 4a, reaction across the length of the friction pad is composed of uniform pressure for $x < L_d a_1$ and $x > L_d + a_2$, while point reactions P_1 and P_2 act at $x = L_d a_1$ and $x = L_d + a_2$ respectively. To calculate the deflections of the driver beam, these loads can be reduced to an effective load and moment P_h and M_h acting at the hinge, as shown in Fig. 4b. Friction pad voltages corresponding to the loads required for a given q are represented by V_p . Electrostatic instabilities [16] in the friction pad region are neglected here. They are not catastrophic because the



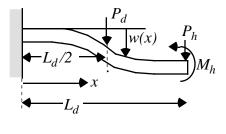


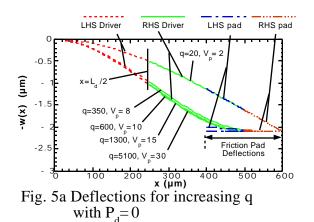
Fig. 4a Beam model used to quantify deflections.

Fig. 4b Transformation to model driver beam.

friction pad acts as a stop. The bending stiffness of the friction pad beam is approximately doubled by the narrow thick poly 2/3 stack at its center (Fig. 3b). This doubling was incorporated in the simulations, but changed the quantitative trends only in detail. To solve for the deflections, the four governing equations for the left and right side of the driver beam and friction pad respectively were expressed. Then, at a given loading, boundary conditions were applied. This gave four equations with four unknowns, which were solved iteratively. Inextensibility of the driver beam was assumed in the calculations.

3.1 EFFECT OF FRICTION PAD LOADING, q

Two simulations were carried out. In the first, the friction pad was loaded with increasing values of q, as represented in Fig. 5. Fig. 5a shows the deflections of the driver pad as well as the friction pad. Fig. 5b shows a close-up in the vicinity of the friction pad. At q=20 N/m² (2V), the friction pad just touches the substrate at its right extreme. As q is increased to 350 N/m² (8V), the slope of the right hand side of the friction pad becomes 0, but the left hand side is not yet in contact. The large increase in q from 20 to 350 N/m² is because large bending resistance in the friction pad must be overcome. Increasing q to 600 N/m² (10V), the left hand side of the friction pad comes into contact with the substrate. At q=1300 N/m² (15V), the slope of the friction pad becomes 0 at its left end. Observe also that the contact in the right hand of the friction pad has increased considerably - a_l has decreased to 29 μ m. Further increases in q reduce both a_l and a_2 . At q=5100 N/m² (30V), a_l has decreased to 49 μ m and a_2 to about 14 μ m.



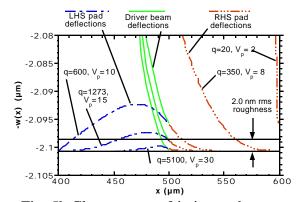
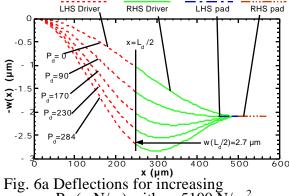


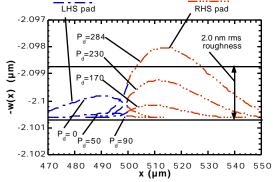
Fig. 5b Close-up near friction pad

Therefore, we have nearly constant pressure along the length of the friction pad for sufficiently high q. Contact mechanics of rough surfaces [18] can be invoked to understand the pressure modulation in more detail.

3.2 EFFECT OF DRIVER PAD LOADING, P_d

In the second simulation, the effect of the driver beam force P_d on driver and friction pad deflections at q=5100 N/m² was studied. The results are graphed in Fig. 6. In Fig. 6a, the maximum deflection occurs at P_d =284 mN/m. This is because for P_d =0, the center point of the driver is (6-1.04)=4.96 μ m above the substrate. It can deflect one third of this distance before destructive electrostatic instability, i.e., 1.66 μ m. Therefore, the maximum deflection is (1.04+1.66)=2.70 μ m at $X = L_d/2$. This limits the total slip of the device, according to Eq. (1).





Solution for increasing P_d (mN/m) with $q=5100 \text{ N/m}^2$ Fig. 6b Close-up in friction pad area

In Fig. 6b, a close-up of Fig. 6a in the friction pad area, a_l is greater than a_2 for $P_d < 90$ mN/m because the driver beam rotation at $x = L_d$ is positive. At $P_d = 90$ mN/m, both a_l and a_2 are zero (independent of q). Effectively only a small point load operates at $x = L_d$; the moment vanishes. For $P_d > 90$ mN/m, a_l is less than a_2 as the driver beam rotation at $x = L_d$ rotates counterclockwise to become negative. Note that the pad deflections continue to be less than the rms roughness, except at the largest value of $P_d = 284$ mN/m. Therefore, the modulation of pressure as P_d cycles continues to be small, according to the above discussion. In order to minimize the effect of the modulation, most devices were built with pad length $L_p = 600$ µm rather than 200 µm. This assures that the pad has uniform distribution over at least 520 µm, i.e. 87% of the area is contacting at pressure q = 5100 N/m² during any part of the cycle.

3.3 RELATIVE SLIP AND TOTAL FRICTION LOAD

Assuming inextensibility of the driver beam, the relative slip of the friction pad vs. P_d can be calculated from the arc length formula, and is plotted in Fig. 7 for q=5100 N/m². The slip increases with the square of P_d , as expected from Eq. (1). The total frictional (normal) load consists of the distributed load q times the area of the

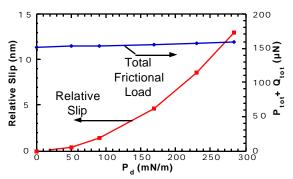


Fig. 7 Relative Slip and Total Normal Load vs. P_d

electrostatic wings, and the sum of point reactions P_1 and P_2 times the width of the electrostatic wings. Their sum must increase as P_d increases. However, variation of the total frictional load is less than 5% because the normal loading is dominated by q, which is independently applied. At P_d =284, the maximum slip is approximately 13 nm. This is the maximum slip possible, and is nearly attainable for reasonably low axial force.

The axial load which the driver beam must develop in order to cause slip of the friction pad is the product of the coefficient of friction and the total frictional load. While the slip is small, the driver beam can develop very high axial loads, on the order of several millinewtons. Therefore, it can induce slip of the friction pad over a wide range of coefficient of friction as well as normal load. With q=5100 N/m², the pressure on the slider pad is 5100*(50/3)=0.085 MPa (W_p =50 μ m, and the width at the bottom of the friction pad is 3 μ m). In principle this can be increased; with a pad voltage of 200V, the applied pressure would be 4 MPa. Another order of magnitude increase in pressure may be possible by reducing the Sac Ox 3 thickness, or by designing the friction pad such that it comes into contact with poly 0 only occasionally along its length.

To summarize, modeling results indicate that with the hinged pad structure, above a reasonably small value of q, the normal load is controllable, nearly evenly distributed and nearly constant along the length of the friction pad as the driver beam oscillates through its cycle. The slip is small, but perhaps sufficient to allow measurement of the cof. In principle, this device can be tested both statically and dynamically, yielding cof data over a wide experimental pressure and velocity space [19].

4. FABRICATION, TESTING AND SIMULATION

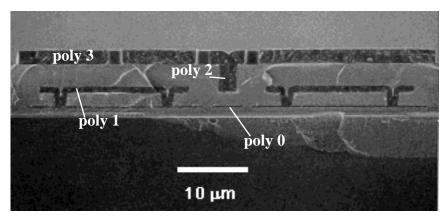


Fig. 8 SEM cross-section of the friction pad. (Compare to Fig. 3b)

(a) OY OY

| driver | friction pad

(b) OY 3Y

(c) OY 10Y

(d) OY 25Y

100 µm

Fig. 9 Pulling down the friction pad with V_n.

The devices were fabricated according to the Sandia multi-level polysilicon surface micromachining process [20]. An SEM cross-section of the friction pad is shown in Fig. 8. By comparing to Fig. 3b, the structure appears to have been successfully realized. In Fig. 8, note that the poly 3 is flat, in spite of the complicated topography beneath it. This can be achieved because our process includes chemical mechanical polishing (CMP) of the Sac Ox 3

layer. The width of the region where the slider pad makes contact with the poly 0 is 3 μ m. This is dictated by the 2.0 μ m minimum width of the Sac Ox 3 cut, as well as alignment tolerances between poly 3 and poly 2.

Devices were released in 1:1 HCl:HF, transferred to H₂O₂ and freed by supercritical CO₂ drying [21]. After the H₂O₂ treatment, the surface is nominally hydrophilic, and a 1 nm oxide covers the surface. Electrical actuation performed under an interferometric microscope (monochromatic green light with =547 nm), such that deflections could be assessed. In Fig. 9, we show results of the effect of pad voltage on the deflections, with 0V on the driver beam. With no voltage applied, we see that the structure is not flat each fringe represents /2=274 nm. By focusing up and down, we could determine that the structures are curved up slightly. This is due to the stress gradient in the polysilicon. The driver beam shows small curvature from the stress gradient, while the curvature in the friction pad is larger. In the friction pad area, a conformal poly 3 deposition fills in 4 of the 6 µm height. (Poly 2 has negligible strain gradient, as could

be determined by observing cantilever beams). Apparently due to the poly 3 being distributed over a 4 μ m thickness, the strain gradient in the friction pad is larger than in the driver beam.

By applying 3V, the friction pad is brought into contact with the substrate, Fig. 9b. At 10V, it is flat along most of its length, as seen in Fig. 9c. Finally, at 25V, the beam is substantially flat. These results are in good qualitative agreement with the spirit of the calculations presented in Fig. 5. The main reason for the discrepancy in comparing the detailed deformations is due to the strain gradient of the poly 3.

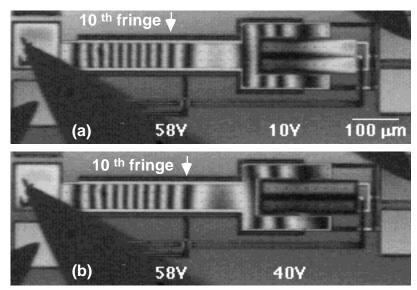


Fig. 10 Driver beam deflections for two different pad voltages

By now inducing driver beam deflections at different driver pad voltages, we can test whether the friction pad induces resistance to slip. For these tests, pad voltage was first applied. Then driver voltage was increased until the driver beam was near pull-in. After a given test, both voltages were relaxed. Usually, the friction pad freed itself from the substrate - adhesive forces were relatively low. In Fig. 10, beam deflections for V_d =58 and for V_p =10V and 40V respectively are shown. Here, the length of the friction pad is 200 µm rather than 600 µm as in Fig. 9. Note that in Fig. 10a, there are approximately eleven fringes from the support post on the left hand side,

while in Fig. 10b, there are only ten fringes. Therefore, comparison of the inteferograms in Figs. 10a and 10b suggests qualitatively that there is a difference in the slip for the two cases of V_p =10V and 40V, because the same driver voltage produces dissimilar deflection profiles.

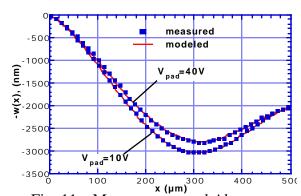


Fig. 11a Measurement and Abacus modeling for data in Fig. 10a

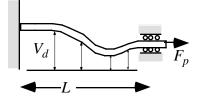


Fig. 11b Schematic of model to match measured deflections

To obtain a quantitative value of the slip, the deflections are first deduced from the fringe data. Linescans were taken along the driver beam from the pad to the slider, and also along one of the forked sections. Because the last segment of the driver beam near the slider and the beginning segment of the fork overlap in x, these two sections were superposed to obtain the total deflection, as shown in Fig. 11a.

Numerical simulation is required to model the deflections because of charge redistribution along the length of the driver beam. The situation modeled is shown in Fig. 11b, where the axial load due to the friction is represented by F_p . To infer slip distance, nonlinear finite element beam models were developed in Abaqus [22] to

match the experimental data. The distributed electrostatic force was accurately modeled as a nonlinear deformation dependent capacitive loading, including Osterberg's fringing field correction [23].

In order to obtain reasonable agreement with the data, the compliance of the support post and the hinge could not be ignored. Rather than estimating this compliance from the geometric structure, the slope near the extremes was measured and included in the modeling boundary conditions. Driver voltage V_d was then applied, and force F_p was increased until the deflections were matched. We see in Fig. 11a that excellent agreement between the simulation and the data is achieved.

Table 1- Calculated parameters from the modeling

$V_{p}\left(\mathbf{V}\right)$	Slip (nm)	$F_p(\mu N)$	$F_n(\mu N)$	cof
10	-4.56	350	45	7.8
40	0.73	390	127	3.1

As seen in Table 1, the modeling results indeed indicate there is a difference in slip of approximately 5 nm between the two cases. The values are relative to the slip after the pad has been brought into contact by pad voltage, and are negative for slip to the left. Slip to the right is not expected, therefore the value of 0.73 nm (which may be slightly off due to experimental error) for V_p =40V probably indicates that the pad has not initiated slip. The values for F_p do not differ greatly. This apparently indicates that for V_p =10V, F_p 350 μ N is required to initiate slip, while for V_p =40V, a value of F_p =390 μ N is insufficient.

Normal force F_n in Table 1 is computed from sum of the point reaction force, 40 μ N, and the distributed force. For V_p =10V, most of the contribution is from the point loading, and the distribution of pressure is rather non-uniform. The pad is in contact only to the left of the hinge, therefore the approximate pressure is ~150 KPa. However, over small variations in pressure, the cof is not generally expected to vary greatly. Keeping this in mind, the apparent cof~8 is somewhat high compared to previous results. For V_p =10V, cof=7.8. This is a lower bound, because it is possible that F_p must increase to move the pad further. The value compares to cof=2 measured for a supercritically dried surface in ref. [13], and cof=5 in ref. [14]. Further study is required to understand this high value. At V_p =10V, V_d =58V is very near the pull-in voltage of the device.

For V_p =40V the pad is in contact along its entire length, and the value of cof=3.1 is a lower bound because the slip apparently has not yet initiated. If the cof is truly 8, no slip is expected before pull-in at V_p =40V. Such a high coefficient of friction limits the usage of this device as currently designed. Greater slip amplitude is possible by the principle of leveraged bending [24], and has been implemented in our next design. Calculations indicate the potential slip can be doubled at the expense of greater driver voltage. Also, we will apply molecular coatings [25] to these devices to lower the coefficient of friction in subsequent measurements.

A problem encountered in our current design is in the symmetry of the friction pad. As seen in Figs. 3b and 8, the pad is loaded symmetrically, which theoretically will give equal loading from each wing. However, a small difference due to geometry after etch or misalignment of poly 3 to poly 0 will cause the force to be unequal on the two sides, giving rise to positive feedback. This results in toppling of the device when the torsional resistance of the driver beam is overwhelmed. Depending on the device, the voltage on the friction pad has been limited to 30-50V maximum. Our follow-up design will employ a more stable friction pad configuration.

5. SUMMARY AND CONCLUSIONS

We have designed, modeled, fabricated and performed initial test measurements on a new structure to measure friction in micromachining. The device consists of a cantilevered forked beam and a friction pad attached via a hinge. The placement of the hinge is crucial to obtaining a well known and constant pressure distribution in the device. Compared to comb drive configurations, the current structure has a larger pressure range and occupies a much smaller area at the expense of range in slip. Furthermore, it has a very large velocity range [19]. Static deflections on the device were measured and modeled using Abaqus. With the oxide coating, slip of 5 nm was inferred shortly before pull-in. The observed $cof \sim 8$ limits the slip range due to stretching of the driver beam. The cof can be reduced by applying molecular coatings, enhancing the usefulness of the present device. To improve on the device, increased slip by leveraged bending and a more stable friction pad configuration will be implemented.

6. ACKNOWLEDGEMENTS

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